The $t \to cH$ decay width in the standard model.

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Abstract

The $t \to cH$ decay width has been computed in the standard model with a light Higgs boson. The corresponding branching fraction has been found to be in the range $B(t \to cH) \simeq 10^{-13} \div 10^{-14}$ for $M_Z \lesssim m_H \lesssim 2M_W$. Our results correct the numerical evaluation usually quoted in the literature.

The one-loop flavor-changing transitions, $t \to cg$, $t \to c\gamma$, $t \to cZ$ and $t \to cH$, are particularly interesting, among the top quark rare decays. Indeed, new physics, such as supersymmetry, an extended Higgs sector and heavier-fermion families could conspicuously affect the rates for this decays. In the standard model (SM), these processes are in general quite suppressed due to the Glashow-Iliopoulos-Maiani (GIM) mechanism, controlled by the light masses of the b, s, d quarks circulating in the loop. The corresponding branching fractions $B_i = \Gamma_i/\Gamma_T$ are further decreased by the large total decay width Γ_T of the top quark. The complete calculations of the one-loop flavour-changing top decays have been performed, before the top quark experimental observation, in the paper by Eilam, Hewett and Soni [1] (also based on Eilam, Haeri and Soni [2]). Assuming $m_t = 175 \text{GeV}$, the value of the total width $\Gamma_T \simeq \Gamma(t \to bW)$ is $\Gamma_T \simeq 1.55 \text{ GeV}$, and one gets from ref. [1]

$$B(t \to cg) \simeq 4 \cdot 10^{-11}, \quad B(t \to c\gamma) \simeq 5 \cdot 10^{-13}, \quad B(t \to cZ) \simeq 1.3 \cdot 10^{-13}.$$
 (1)

In the same ref. [1], a much larger branching fraction for the decay $t \to cH$ is presented as function of the top and Higgs masses (in Fig. 1 the relevant Feynman graphs for this channel are shown). For $m_t \simeq 175$ GeV and 40 GeV $\lesssim m_H \lesssim 2M_W$, the value

$$B(t \to cH) \simeq 10^{-7} \div 10^{-8}$$
 (2)

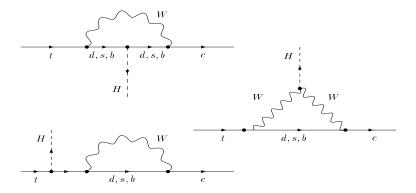


Figure 1: Feynman graphs for the decay $t \to cH$ in the unitary gauge ($m_c = 0$ is assumed).

is obtained, by means of the analytical formulae presented in ref. [2] for the fourthgeneration quark decay $b' \to bH$, in a theoretical framework assuming four flavour families. Such relatively large values for $B(t \to cH)$ look surprising, since the topology of the Feynman graphs for the different one-loop channels is similar, and a GIM suppression, governed by the down-type quark masses, is acting in all the decays.

In order to clarify the situation, we recomputed from scratch the complete analytical decay width for $t \to cH$, as described in [3]. The corresponding numerical results for $B(t \to cH)$, when $m_t = 175 \, \text{GeV}$ and $\Gamma(t \to bW) \simeq 1.55 \, \text{GeV}$, are reported in Table 1. We used $M_W = 80.3 \, \text{GeV}$, $m_b = 5 \, \text{GeV}$, $m_s = 0.2 \, \text{GeV}$, and for the Kobayashi-Maskawa matrix elements $|V_{tb}^*V_{cb}| = 0.04$. Furthermore, we assumed $|V_{ts}^*V_{cs}| = |V_{tb}^*V_{cb}|$. As a consequence, the m_d dependence in the amplitude drops out.

Our results are several orders of magnitude smaller than the ones reported in the literature. In particular, for $m_H \simeq M_Z$ we obtain

$$B_{new}(t \to cH) \simeq 1.2 \cdot 10^{-13}$$
 (3)

to be compared with the corresponding value presented in ref. [1]

$$B_{old}(t \to cH) \simeq 6 \cdot 10^{-8}. \tag{4}$$

In order to trace back the source of this inconsistency, we performed a thorough study of the analytical formula in eq. (3) of ref. [2], for the decay width of the fourth-family down-type quark $b' \to bH$, that is the basis for the numerical evaluation of $B(t \to cH)$

presented in ref. [1]. The result of this study was that we agreed with the analytical computation in [2], but we disagreed with the numerical evaluation of $B(t \to cH)$ in [1].

The explanation for this situation can be ascribed to some error in the computer code used by the authors of ref. [1] to work out their Fig. 3. This explanation has been confirmed to us by one of the authors of ref. [1] (J.L.H.), and by the erratum appeared consequently [4], whose evaluation we now completely agree with.

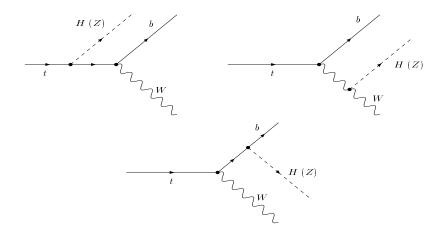


Figure 2: Feynman graphs for the decay $t \to bWH$ $(t \to bWZ)$.

In the following we give some euristic considerations useful in order to understand the correct order of magnitude of the rate for the decay $t \to cH$. The comparison between the rates for $t \to cZ$ and $t \to cH$ and the corresponding rates for the tree-level decays $t \to bWZ$ and $t \to bWH$, when $m_H \simeq M_Z$ can give some hint on this order of magnitude. In fact, the latter channels can be considered a sort of lower-order parent processes for the one-loop decays, as can be seen in Fig. 2, where the relevant Feynman graphs are shown. Indeed, the Feynman graphs for $t \to cZ$ and $t \to cH$ can be obtained by recombining the final b quark and W into a c quark in the three-body decays $t \to bWZ$ and $t \to bWH$, respectively, and by adding analogous contributions where the b quark is replaced by the s and d quarks. Then, the depletion of the $t \to cH$ rate with respect to the parent $t \to bWH$ rate is expected to be of the same order of magnitude of the depletion of $t \to cZ$ with respect to $t \to bWZ$, for $m_H \simeq M_Z$. In fact, the GIM mechanism acts in a similar way in the one-loop decays into H and Z.

The $t \to bWZ$ and $t \to bWH$ decay rates have been computed, taking into account crucial W and Z finite-width effects, in ref. [5]. For $m_H \simeq M_Z$, the two widths are

$m_H (GeV)$	$B(t \to cH)$
80	$0.1532 \cdot 10^{-12}$
90	$0.1169 \cdot 10^{-12}$
100	$0.8777 \cdot 10^{-13}$
110	$0.6452 \cdot 10^{-13}$
120	$0.4605 \cdot 10^{-13}$
130	$0.3146 \cdot 10^{-13}$
140	$0.1998 \cdot 10^{-13}$
150	$0.1105 \cdot 10^{-13}$
160	$0.4410 \cdot 10^{-14}$

Table 1: Branching ratio for the decay $t\to cH$ versus m_H . We assume $m_t=175{\rm GeV}$ and $m_c=1.5{\rm GeV}$.

comparable. In particular, for $m_t \simeq 175 \text{GeV}$, one has [5]

$$B(t \to bWZ) \simeq 6 \cdot 10^{-7}$$
 $B(t \to bWH) \simeq 3 \cdot 10^{-7}$. (5)

From [1], $B(t \to cH) \simeq 6 \cdot 10^{-8}$ for $m_H \simeq M_Z$. Accordingly, the ratio of the one-loop and tree-level decay rates is

$$r_H \equiv \frac{B(t \to cH)}{B(t \to bWH)} \sim 0.2 \tag{6}$$

to be confronted with

$$r_Z \equiv \frac{B(t \to cZ)}{B(t \to bWZ)} \sim 2 \cdot 10^{-7}.$$
 (7)

On the other hand, r_H and r_Z are related to the quantity

$$\left(\frac{g}{\sqrt{2}}|V_{tb}^*V_{cb}|\frac{m_b^2}{M_W^2}\right)^2 \sim 10^{-8}$$
(8)

(where V_{ij} are the Kobayashi-Maskawa matrix elements) arising from the higher-order in the weak coupling and the GIM suppression mechanism of the one-loop decay width. The large discrepancy between the value of the ratio r_H in eq. (6) and what was expected from the factor in eq. (8), which, on the other hand, is supported by the value of r_Z , was a further indication that the values for $B(t \to cH)$ reported in eq. (2) could be incorrect.

Indeed, the new value of $B(t \to cH)$ in eq. (3) gives $r_H \sim 4 \cdot 10^{-7}$.

In conclusion, we have pointed out that one of the numerical results of ref. [1] establishing a relatively large branching ratio for the decay $t \to cH$ in the SM has been overestimated. The correct numerical estimates are shown in Table 1. We find $B(t \to cH) \simeq 1 \cdot 10^{-13} \div 4 \cdot 10^{-15}$ for $M_Z \lesssim m_H \lesssim 2M_W$. Such a small rate will not be measurable even at the highest luminosity accelerators that are presently conceivable. An eventual experimental signal in the rare t decays will definitely have to be ascribed to some new physics effect.

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